



**GCE AS/A level**

0973/01

**MATHEMATICS – C1**  
**Pure Mathematics**

A.M. MONDAY, 13 January 2014

1 hour 30 minutes

### **ADDITIONAL MATERIALS**

In addition to this examination paper, you will need:

- a 12 page answer book;
- a Formula Booklet.

### **INSTRUCTIONS TO CANDIDATES**

Use black ink or black ball-point pen.

Answer **all** questions.

Sufficient working must be shown to demonstrate the **mathematical** method employed.

Calculators are **not** allowed for this paper.

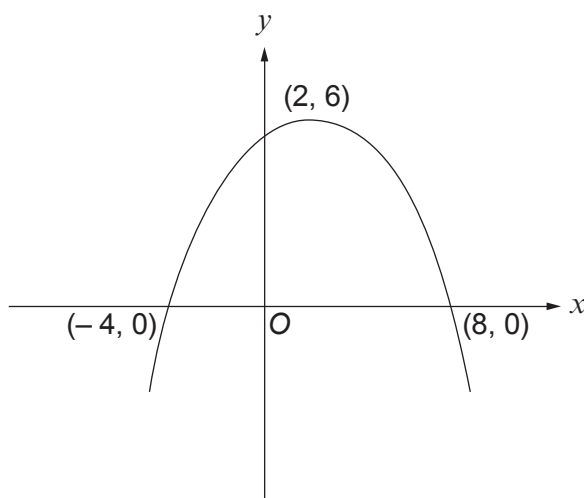
### **INFORMATION FOR CANDIDATES**

The number of marks is given in brackets at the end of each question or part-question.

You are reminded of the necessity for good English and orderly presentation in your answers.

1. The points  $A$  and  $B$  have coordinates  $(6, -2)$  and  $(4, 1)$ , respectively. The line  $L_1$  passes through the point  $B$  and is perpendicular to  $AB$ .
- (a) (i) Find the gradient of  $AB$ .  
 (ii) Find the equation of  $L_1$ . [5]
- (b) The line  $L_2$  passes through  $A$  and has equation  $x - 8y - 22 = 0$ . The lines  $L_1$  and  $L_2$  intersect at the point  $C$ .
- (i) Show that  $C$  has coordinates  $(-2, -3)$ .  
 (ii) Find the coordinates of the mid-point of  $AC$ .  
 (iii) Find the area of triangle  $ABC$ , simplifying your answer. [9]
2. Simplify  $\frac{3\sqrt{3} - 2\sqrt{5}}{2\sqrt{3} + \sqrt{5}}$ . [4]
3. The curve  $C$  has equation  $y = \frac{20}{x} + 2x^2 - 11$ . The point  $P$  has coordinates  $(2, 7)$  and lies on  $C$ . Find the equation of the **normal** to  $C$  at  $P$ . [6]
4. Show that  $x^2 + 1.6x - 24.36$  may be expressed in the form  $(x + p)^2 - 25$ , where  $p$  is a constant whose value is to be found.  
**Hence** solve the quadratic equation  $x^2 + 1.6x - 24.36 = 0$ . [5]
5. (a) **Use the binomial theorem** to express  $(1 + \sqrt{6})^5$  in the form  $a + b\sqrt{6}$ , where  $a, b$  are integers whose values are to be found. [5]  
 (b) The coefficient of  $x^2$  in the expansion of  $(1 + 3x)^n$  is 495. Given that  $n$  is a positive integer, find the value of  $n$ . [3]
6. Given that the quadratic equation
- $$(2k - 3)x^2 + 8x + (2k + 3) = 0$$
- has no real roots, show that  $k$  satisfies an inequality of the form
- $$m - nk^2 < 0,$$
- where  $m, n$  are integers whose values are to be found.
- Hence find the range of values of  $k$  such that the quadratic equation
- $$(2k - 3)x^2 + 8x + (2k + 3) = 0$$
- has no real roots. [6]

7. **Figure 1** shows a sketch of the graph of  $y = f(x)$ . The graph has a maximum point at  $(2, 6)$  and intersects the  $x$ -axis at the points  $(-4, 0)$  and  $(8, 0)$ .



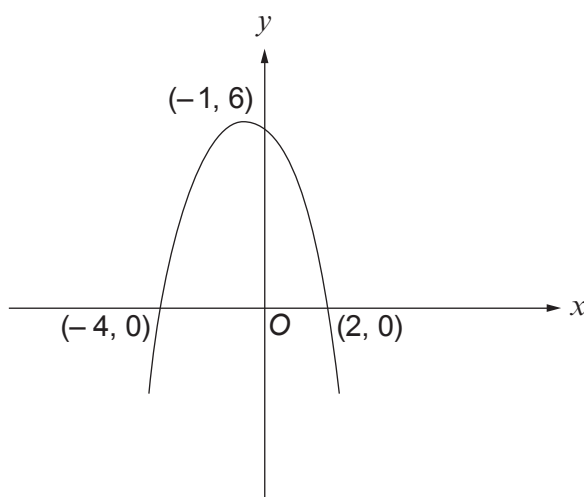
**Figure 1**

- (a) Sketch the graph of  $y = f(x - 3)$ , indicating the coordinates of the stationary point and the coordinates of the points of intersection of the graph with the  $x$ -axis. [3]
- (b) **Figure 2** shows a sketch of the graph having **one** of the following equations with an appropriate value of  $p$ ,  $q$  or  $r$ .

$$y = f(x) + p, \text{ where } p \text{ is a constant}$$

$$y = f(qx), \text{ where } q \text{ is a constant}$$

$$y = rf(x), \text{ where } r \text{ is a constant}$$



**Figure 2**

Write down the equation of the graph sketched in **Figure 2**, together with the value of the corresponding constant. [2]

**TURN OVER**

8. (a) Given that  $y = 7x^2 - 6x - 3$ , find  $\frac{dy}{dx}$  from first principles. [5]

(b) Given that  $y = ax^{\frac{4}{3}} + 24x^{\frac{1}{2}}$  and that  $\frac{dy}{dx} = \frac{11}{2}$  when  $x = 64$ ,  
find the value of the constant  $a$ . [4]

9. (a) When  $ax^3 + 13x^2 - 10x - 24$  is divided by  $x + 3$ , the remainder is  $-39$ .  
Write down an equation satisfied by  $a$  and hence show that  $a = 6$ . [2]

(b) Solve the equation  $6x^3 + 13x^2 - 10x - 24 = 0$ . [6]

10. The curve  $C$  has equation

$$y = -2x^3 + 12x^2 - 18x + 5.$$

(a) Find the coordinates and the nature of each of the stationary points of  $C$ . [6]

(b) Sketch  $C$ , indicating the coordinates of each of the stationary points. [2]

(c) Given that the equation

$$-2x^3 + 12x^2 - 18x + 5 = k$$

has three distinct real roots, find the range of possible values for  $k$ . [2]